



RIIIC

**Stochastic Problem Solving
by Local Computation
based on Self-organization Paradigm**

Yasusi Kanada

Tsukuba Research Center

Real World Computing Partnership

Masao Hirokawa

Advanced Research Laboratory

Hitachi, Ltd.

Problems of real-world computational systems

Introduction

■ Future real-world computational systems are

- ◆ Complex (such as secretary robot brains)
 - “Non-linear,” or
 - Undecomposable into “independent” modules (because of strong interaction between modules)
- ◆ Open and adaptive to real world (i.e., to humans and/or natural systems)
 - Adaptive to unexpected inputs (in a short period of time)
 - humans and natural systems are unpredictable because autonomous and nondeterministic.
 - Adaptive to environmental change (in a long period of time)

■ In development of real-world computational systems

- ◆ No global and complete specifications can be written, because open to real world
- ◆ Top-down design or divide-and-concur method do not work well, because of no complete specification, and complexity.

What is the self-organization paradigm?

■ What is self-organization?

- ◆ An emergent behavior — toward “global order” from local motion
- ◆ We should learn from nature.
 - Natural systems are self-organizing systems.
 - Natural sciences on self-organizing systems:
Dissipative structure theory by Prigogine, *Synergetics* by Haken,
Molecular evolution theory by Eigen,
Autopoiesis theory by Matrana and Varela,
Bio-holonics by Shimizu, Natural and artificial *neural networks*,

■ “Global order” from computation with local information

- ◆ Computation only with local and partial knowledge — no algorithms.
- ◆ Computation only with partial specification! (or no specification?)

■ The knowledge shortage must be covered by

- ◆ Nondeterminism (trial and error, or random selections) in short range.
- ◆ Self-organization in long range. (Nondeterminism is important for self-organization.)

Research goals

■ Long-term research goals

- ◆ To develop a new problem-solving methodology based on a self-organization paradigm.
- ◆ To develop adaptive and open computational systems.

■ We are only at the beginning of research toward these goals.

■ Short-term research objective

- ◆ To establish a computation mechanism and methodology, which are
 - Emergent and nondeterministic
 - Based on local and partial information.

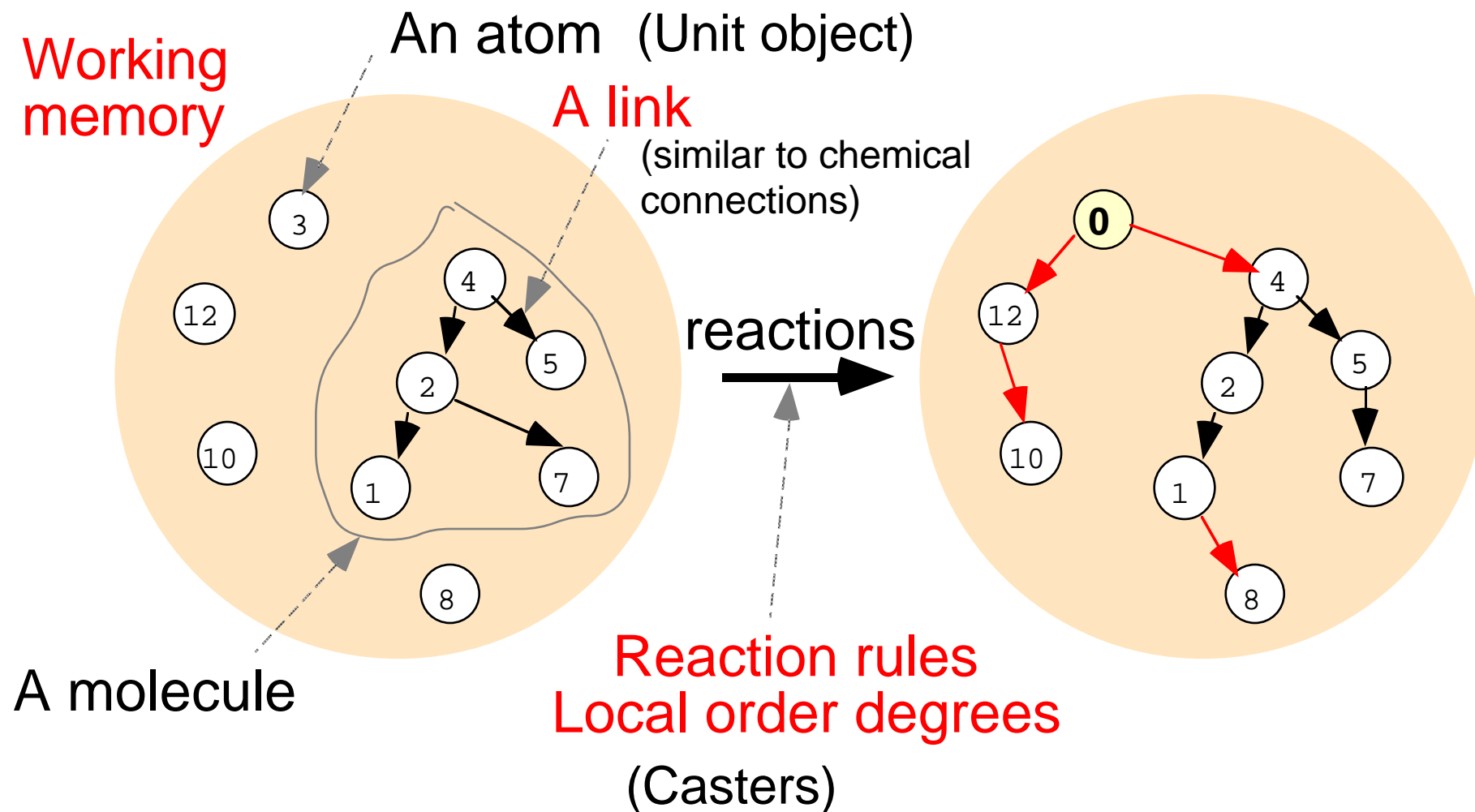
Computation model CCM

A microscopic model of computation

- **We develop a computation model called CCM for self-organizing computation.**
 - ◆ CCM is an abbreviation of “Chemical Casting Model.”
 - ◆ “Chemical” means CCM has an analogy to chemical systems.
 - ◆ “Casting” means programming or computation.
 - I do not use “program” because it means a whole and complete plan.

Components of CCM — 1

Outline



Components of CCM — 2

Casters (Programs) of CCM

■ A caster consists of

- ◆ Local order degrees (LODs)
- ◆ Reaction rules

■ LODs

- ◆ Are local evaluation functions (or negative energy).
 - “Local” means “defined on a small number of data.”
- ◆ Are defined for an atom or between two or more atoms.

■ Reaction rules

- ◆ Change partial (local) state of the working memory.
- ◆ Are written as forward-chaining production rules, such as
 - Chemical reaction formulae.
 - Rules in production systems, used for building expert systems.

Computation process in CCM

■ A reaction

- ◆ An application of a reaction rule is called a reaction.
- ◆ A reaction takes place when
 - There are a rule and a set of data that match the LHS of the rule, and
 - The sum of LODs of the data, concerning the reaction, does not decrease by the reaction.

■ Succession and termination of reactions

- ◆ Reactions occur successively when possible.
 - Their order is nondeterministic (or random) — No limit cycles occur!
- ◆ If no reaction can occur, then the system (temporarily) terminates.
- ◆ The system may begin to work again, when data are modified, removed or added externally.

The N queens problem

Example: the N queens system — 1

■ The N queens problem

- ◆ An extension of the eight queens problem.
- ◆ A problem of finding a layout of N queens on $N \times N$ “chess board,” where a queen does not take each other.

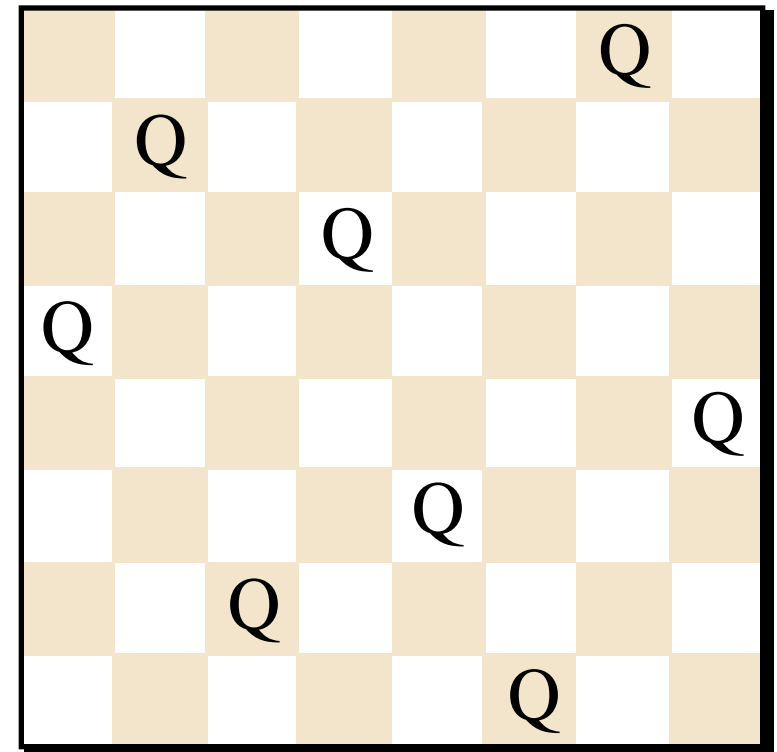
■ The N queens system

- ◆ A computational system to solve the N queens problem in CCM.

■ The reasons that we use the N queens problem

- ◆ We have to start with a simpler system.
- ◆ This system has several characteristics that will probably lead us to a better understanding of complex systems.

A solution of the eight queens problem



How to solve the N queens problem?

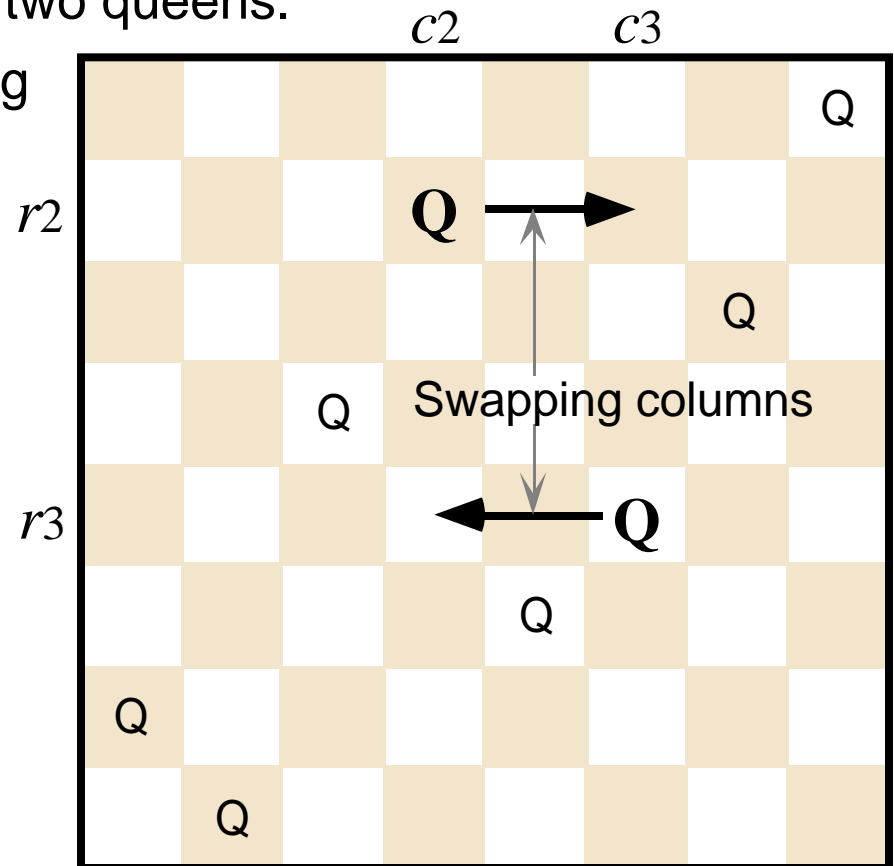
Example: the N queens system — 2

■ Using swap operations

- ◆ A reaction swaps the columns of two queens.
- ◆ To solve the problem by repeating the swaps of different queens.

■ The initial conditions

- ◆ All the queens are put on the board from the beginning.
- ◆ There is only one queen in each row and each column.
 - Example: all the queens can be put on a diagonal line.
 - This condition holds at any time because the reaction preserves it.

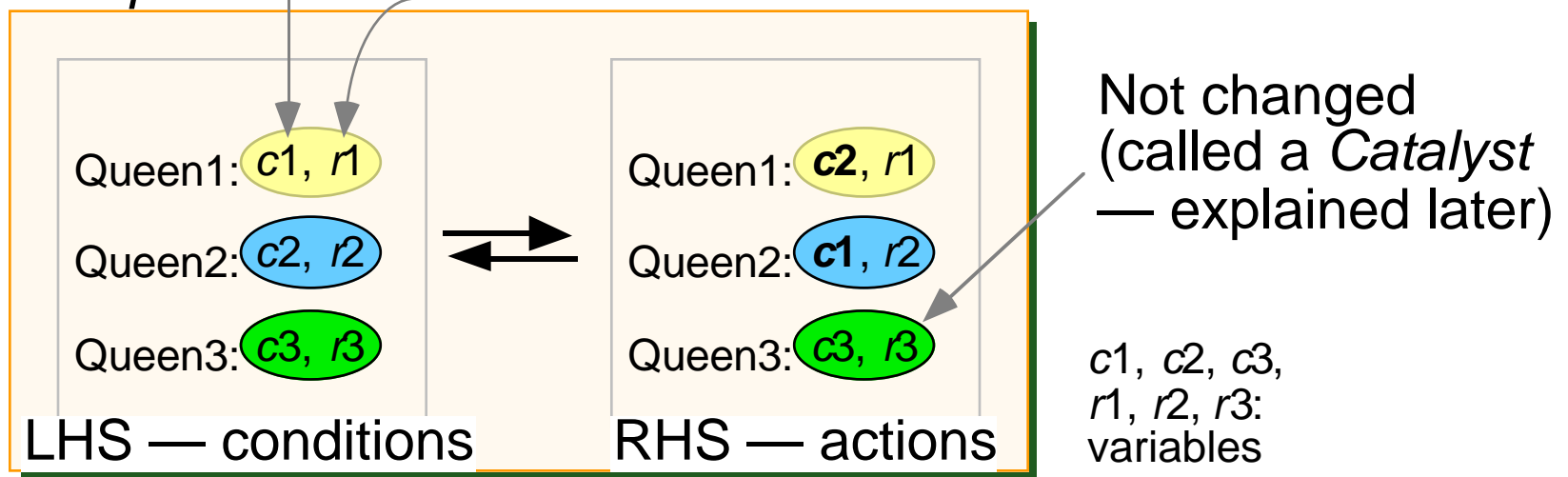


The caster for the N queens system

Example: the N queens system — 3

■ Reaction rule (only one)

rule *Swap* column row : the representation of a queen (coordinates)



■ Local order degree (Mutual order degree)

- ◆ Definition: $o(x, y) = 0$ if $x.column - y.column = x.row - y.row$ or $x.column - y.column = y.row - x.row$,
1 otherwise.

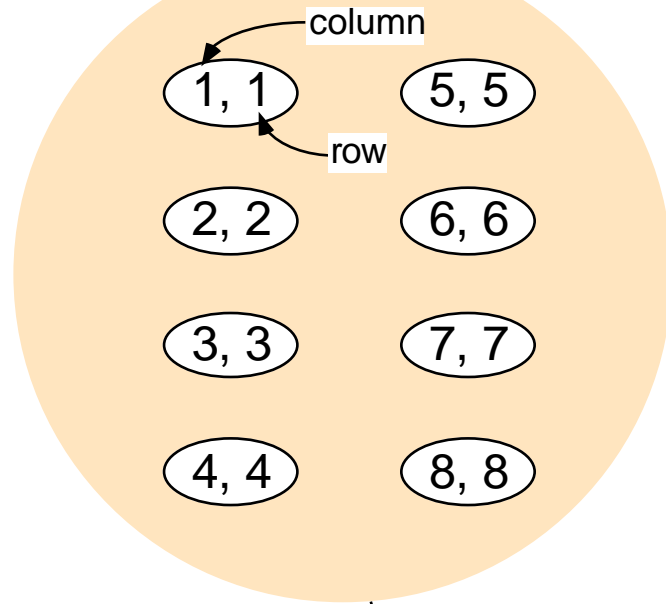
- ◆ Meaning:

If queens x and y are diagonally oriented, then 0. Otherwise, 1.

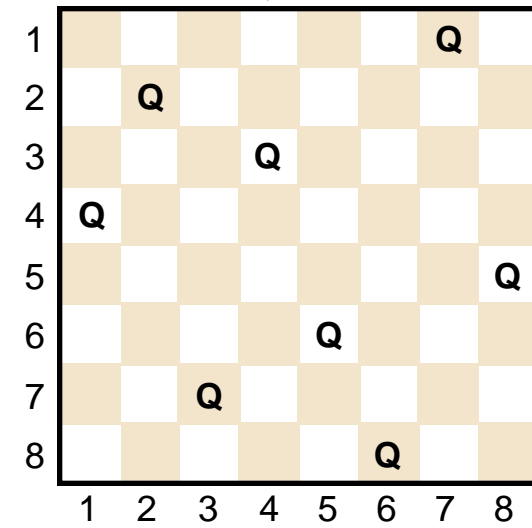
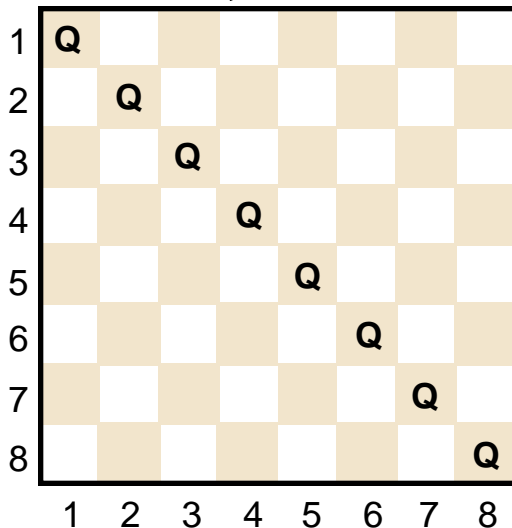
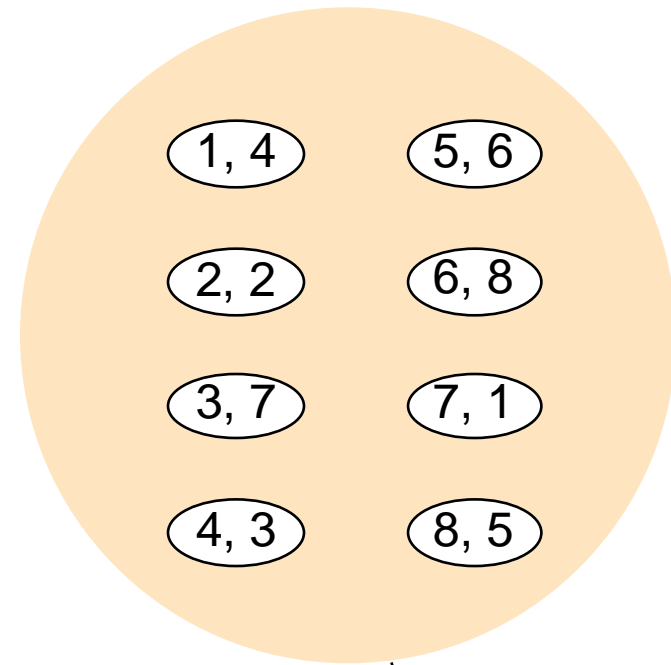
Less ordered
More ordered

Content of working memory for the eight queens

Working memory



Reactions



A more detailed semantics of reactions

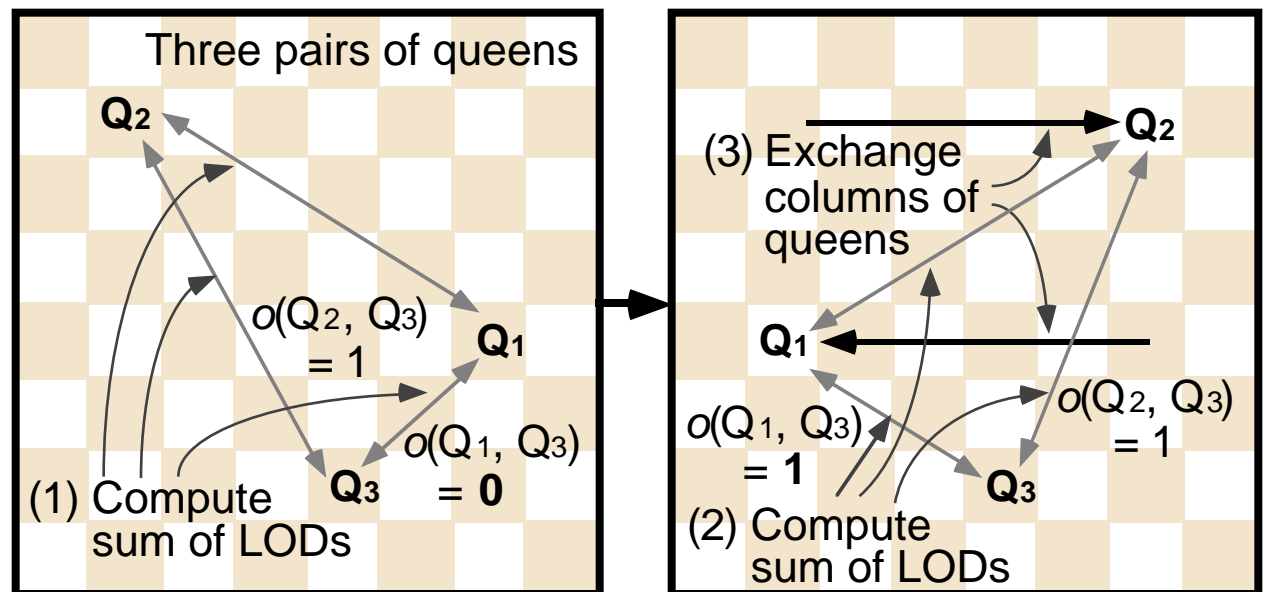
Example: the N queens system — 4

■ Selections of a rule and objects

- ◆ No need to select a rule because there is only one rule.
- ◆ Three queens are *nondeterministically* (randomly) selected and reacted.

■ Computation of order degrees

- ◆ The sums of LODs before and after the reaction are computed (before the reaction).



■ The reason that the catalyst (Q₃) is necessary

- ◆ The sum of LODs is not changed if the rule contains only Q₁ and Q₂, because the LOD between Q₁ and Q₂ is not changed.
 - So the system does not stop when a solution is found.

Performance evaluation — 0*

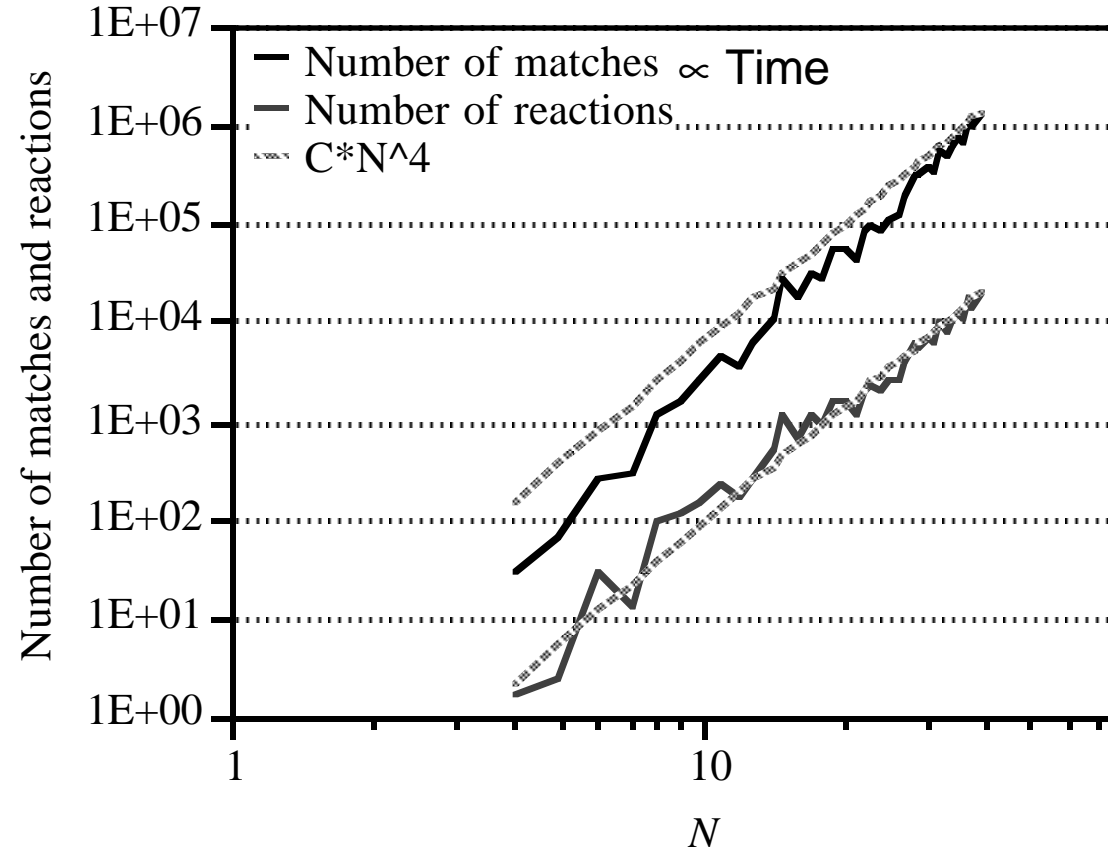
Several conditions of the measurement

- **The performance of the N queens system is measured using SOOC.**
 - ◆ SOOC (Self-Organization-Oriented Computing) is a computation language based on CCM.
- **The initial layouts of queens are random.**
- **All values are averages of ten executions.**

Performance evaluation

Results of the N queens

- **The problems never fail to be solved in our experiments,**
 - ◆ In spite of the stochastic and non-exhaustive search method.
- **The execution time is in polynomial order ($O(N^{4.6})$).**
 - ◆ Much faster than blind backtrack search ($O(e^N)$).
 - ◆ It is slower than more intelligent methods (Yagrom's method — $O(N)$).



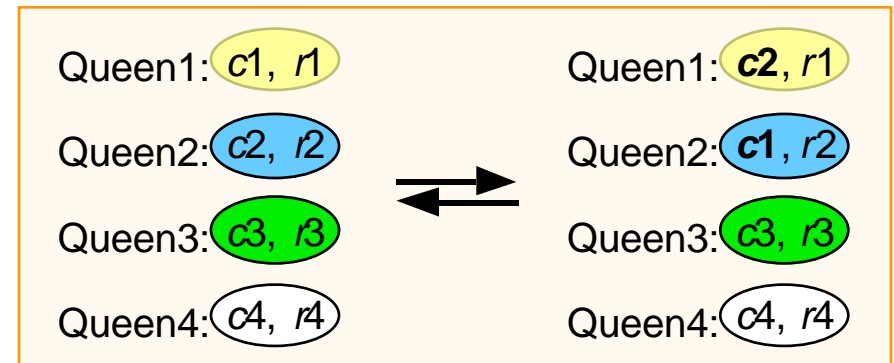
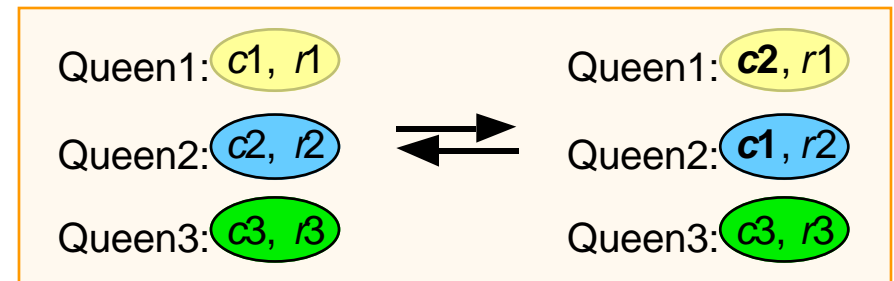
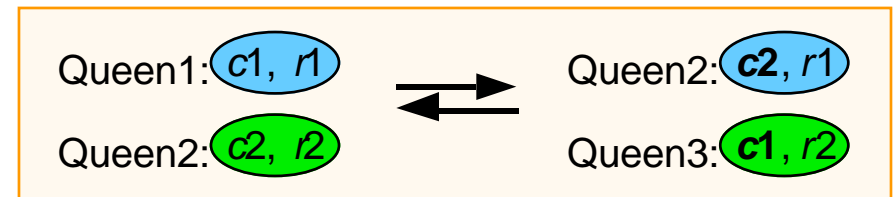
Locality control by catalysts — 1

Variability of locality

- The locality of data reference can be controlled by adding/removing catalysts to rules.

- Versions of the N queens rule

- ◆ A rule with no catalyst ($N_c = 0$):
 - Most local
(minimum data reference)
- ◆ A rule with one catalyst ($N_c = 1$):
- ◆ A rule with two catalysts ($N_c = 2$):
 - Less local
- ◆ A rule with $N - 2$ catalysts ($N_c = N - 2$)
 - Global — all the queens are referred.



Locality control by catalysts — 2

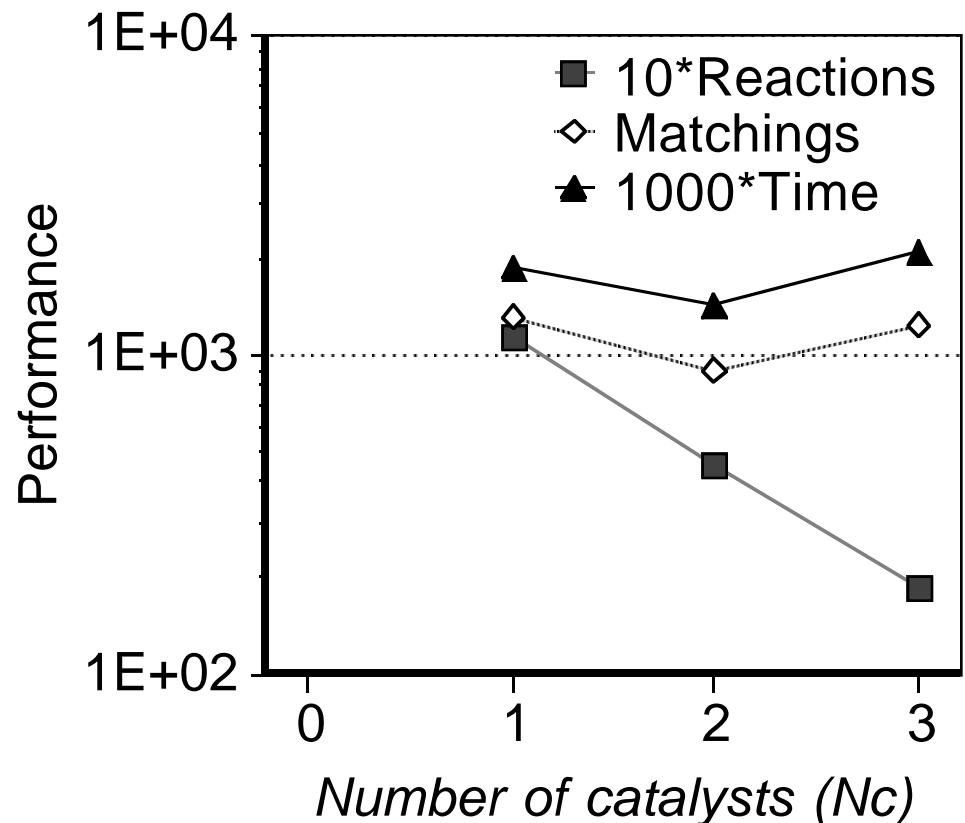
Performance comparisons when changing N_c

■ No catalyst

- ◆ The system does not stop even when a solution is found — because there is no bias toward solutions.
 - The execution time is infinite.

■ One catalyst or more

- ◆ The number of reactions decreases when N_c increases.
- ◆ The execution time is optimum when $N_c = 2$.



Locality control by catalysts — 3

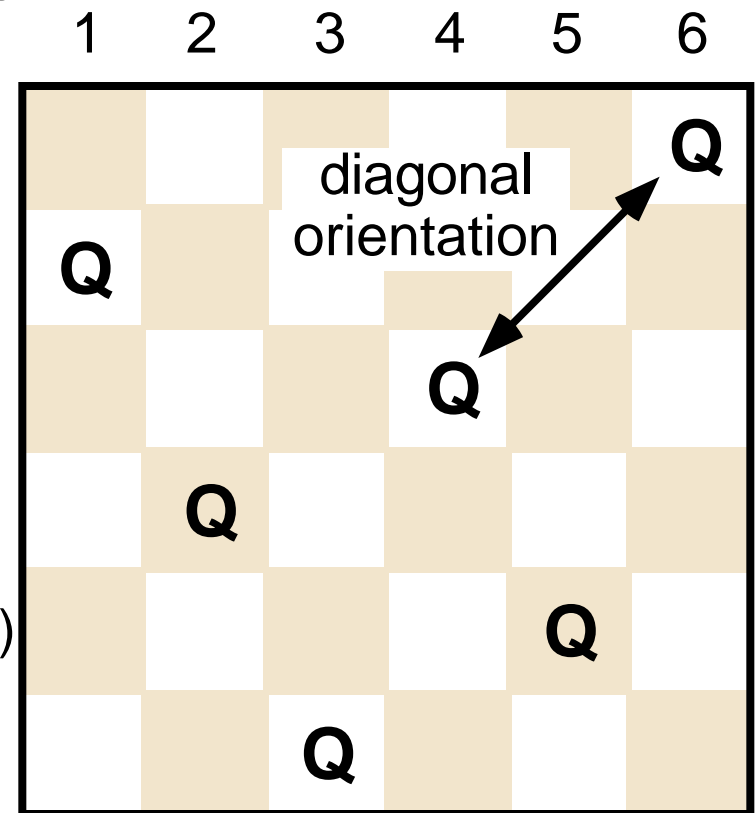
Escaping from “local maxima”

■ No catalyst

- ◆ No bias (complete random walk)
 - no local maxima (of global order degree — the total of LODs (negative total energy)).

■ One catalyst or more

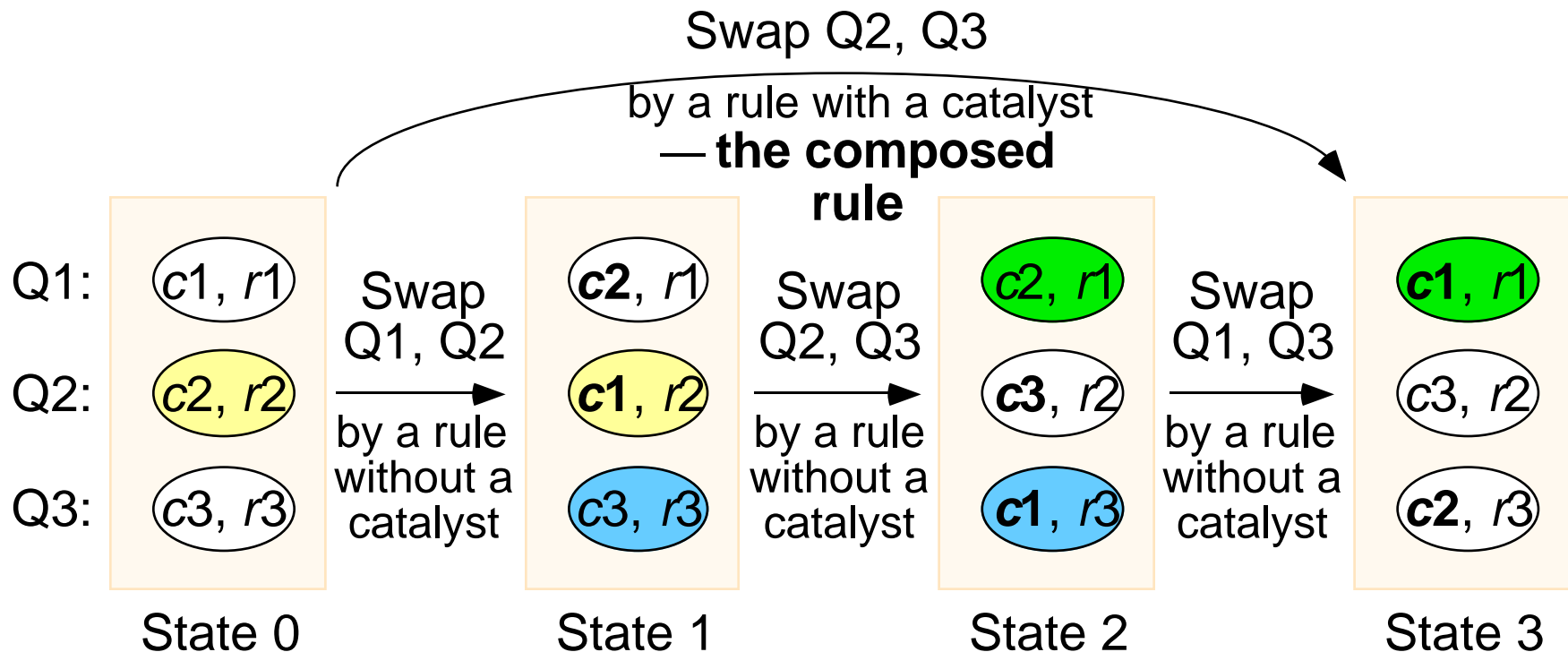
- ◆ There may be local maxima
 - invalid termination.
- ◆ If less catalysts — less chances to fall into a local maximum.
 - Simulated-annealing-like effect.
- ◆ Example: the six queens system
 - No local maxima (are proved to be) exist when $N_c = 1$.
 - Local maxima exist when $N_c = 4$ (global rule).



A local maximum of the six queens system

Locality control by rule composition*

- The locality can also be controlled by composing rules.
- A rule with two or more catalysts may be composed using rules with one catalyst.
 - ◆ Example: the N queens rule with two catalysts can be composed using the rule with one catalyst twice.



Global order degree and its time sequence*

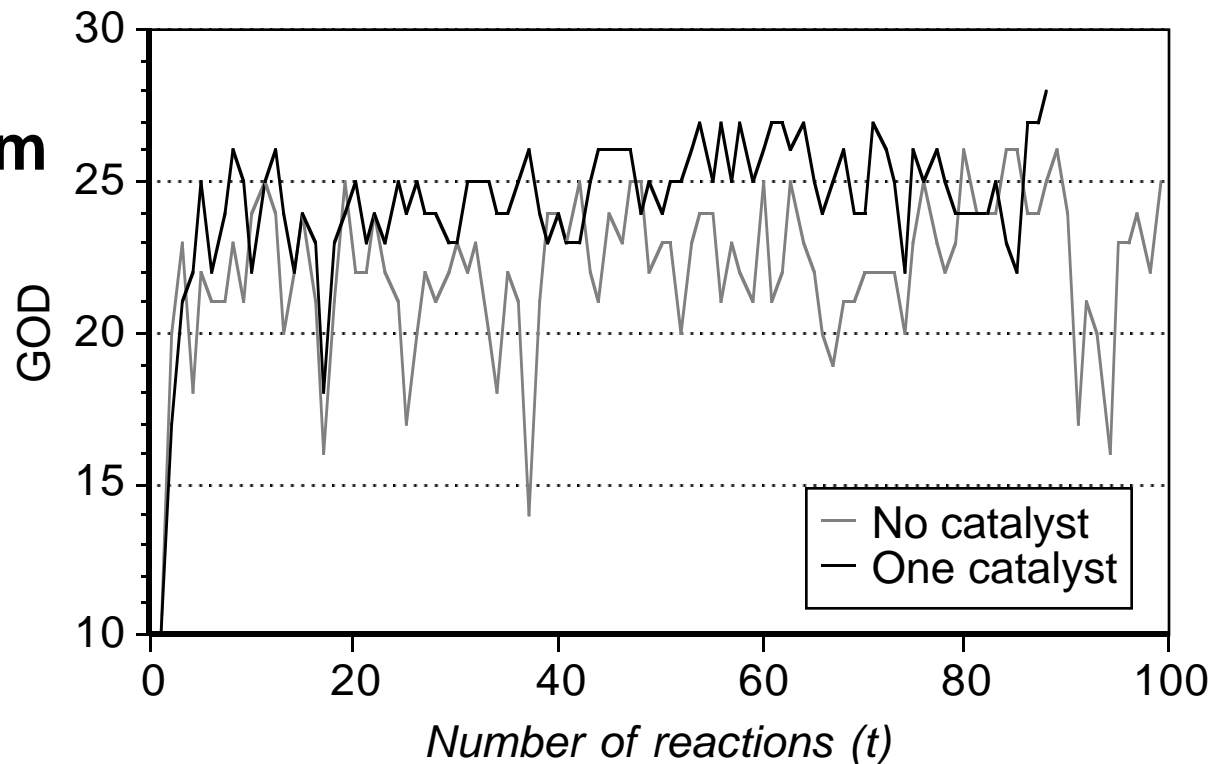
A macroscopic model of computation

■ Global order degree (GOD)

- ◆ GOD is the sum of the LODs of all the atoms (or all pairs of atoms).
- ◆ The GOD is at a maximum at the solutions.

■ An example: the eight queens system

- ◆ $0 \leq \text{GOD} \leq 28$.
- ◆ The initial GOD is 0 — all the queens are on a diagonal line.



Other applications*

■ Current applications of CCM — still far from real world

Classification		Problem	Rules and LODs		Performance	
			Number of rules *	Number of LODs	Time	Solution quality
NP-hard	Optimization	TSP	1	1	$O(N^3)$	97 times optimum out of 100 trials ($N = 10$)
		0-1 Knapsack	1 (or 2)	1	$O(N^2)$	45 times optimum out of 100 trials ($N = 20$)
	Constraint satisfaction	N Queens	1	1	$O(N^{4.6})$	—
		Graph (or map) coloring	1	1	—	—
P-hard	Sorting	1	1	$O(N^2)$	—	

* Rules for working memory initialization are not counted.

■ The above problems are solved using very simple casters.

Summary

■ I explained the self-organization paradigm.

- ◆ Self-organization — “global order” from computation with local information

■ We proposed a computation model CCM for self-organizing computation.

- ◆ Problems can be solved using one or a few simple production rules and evaluation functions.
- ◆ Both production rules and evaluation functions works locally — i.e., on a small number of objects.
- ◆ Locality of data reference can be controlled
 - By adding/removing catalysts and composing rules.
 - Local maxima can be avoided by changing locality.
 - Efficiency of searches can be controlled by changing locality.

Future work

■ Toward open systems

- ◆ To develop CCM-based open systems
 - Constraint satisfaction or optimization problems are basically closed.
- ◆ To observe and to analyze more complex emergent properties in those systems.

■ Self-referential systems: a type of self-organizing systems

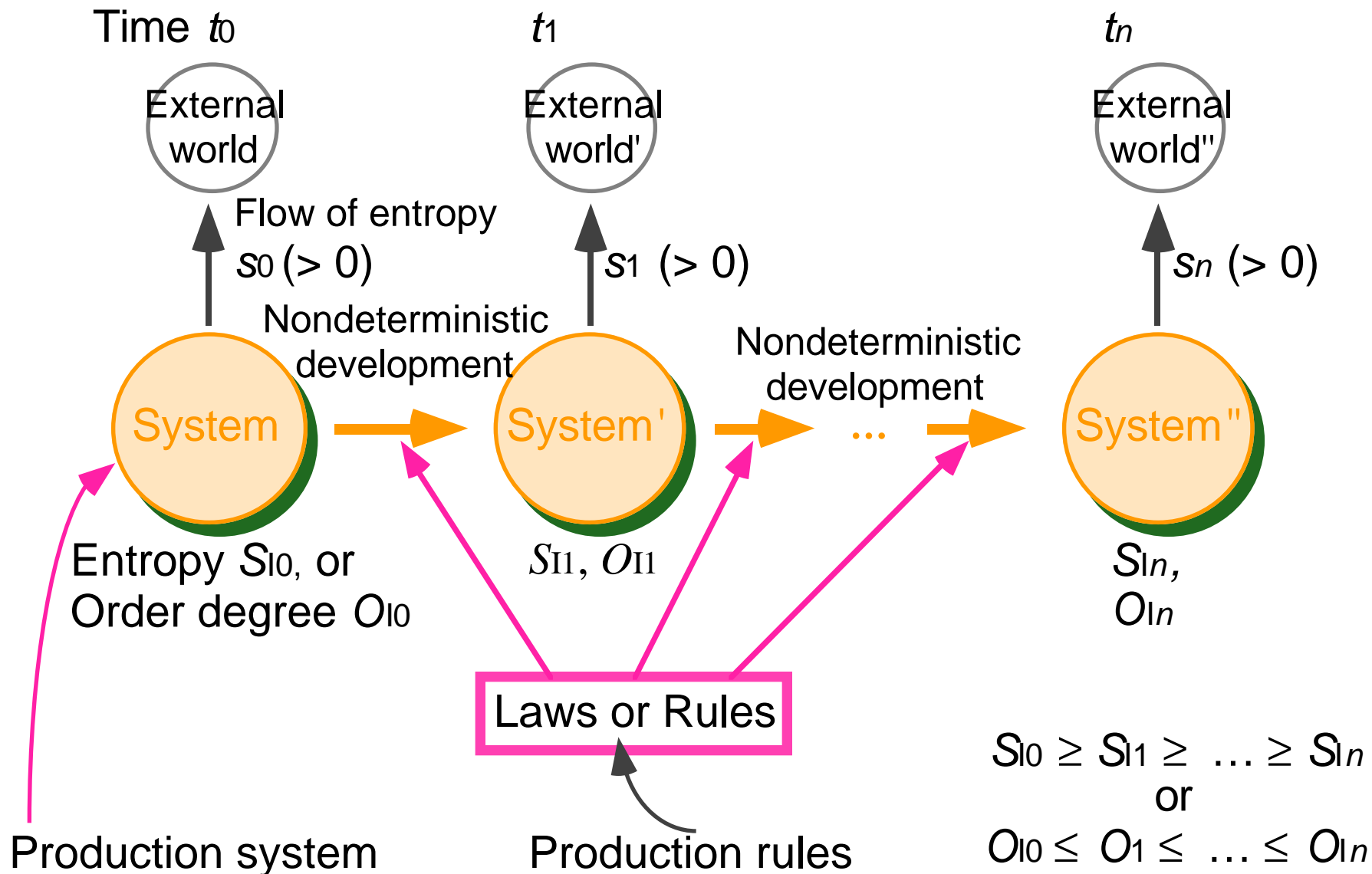
- ◆ To study self-modifying rules and LODs.
- ◆ To study self-modifying targets of computation.
- ◆ CCM must be enhanced to express self-references.

Contents*

- Introduction — the self-organization paradigm
- Computation model CCM (Chemical Casting Model)
- Example: the N queens system
- Locality control of data references
- Other examples
- Summary and future work

A model of self-organizing systems — 1*

A macroscopic model



A model of self-organizing systems — 2*

- **This model can be applied to a wide range of self-organizing systems, such as**
 - ◆ Our target self-organizing computational system.
 - ◆ A thermodynamic system that generates a dissipative structure.
- **The growth of a self-organizing system is autonomous, and, thus, its behavior is unpredictable, or it is observed as nondeterministic or driven by noise that comes from the outside of the system.**

Data in CCM*

Components of CCM — 3

■ Working memory

- ◆ The set of objects to which the rules apply.

■ Atoms

- ◆ Atoms are unit objects.
- ◆ Atoms have internal state.

■ Links

- ◆ Links are connectors of atoms.
- ◆ Links may have directions.
- ◆ Links may have labels (names).

Order of reactions*

■ Order of reactions is nondeterministic.

- ◆ Random, or independent of the problem logic.

■ Different reaction orders may cause different results.

- ◆ All possible results will be as expected
— because induced by the LODs.

■ Scheduling strategies

- ◆ Are specified by the user, or determined by the system.
- ◆ Control the selections macroscopically.
- ◆ Are similar to conflict resolution strategies in conventional production systems.

Types of scheduling strategies*

■ Mathematical random strategies (MRS)

- ◆ Use pseudo-random numbers.
- ◆ Do not cause limit cycles, even if the user pays no attention.
- ◆ Are the standard strategies.

■ Systematic strategies (SS)

- ◆ Use systematic methods — independent of the problem logic.
- ◆ May cause limit cycles (infinite loops).

■ Parallel strategies

Computation as Markov process*

- **Computation can be regarded as a stochastic process in CCM even when an S strategy is used.**
- **Three states during the computation of CCM.**
 - ◆ Strongly non-stationary state
 - The state in which the probability distribution rapidly changes when a reaction occurs.
 - ◆ Quasi-stationary state
 - The state that the probability of the solution state, $p(g_{\max})$, increases when a reaction occurs, where g_{\max} is the maximum value of the GOD (= NC2), but that the ratio of other states, $p(g)/(1 - p(g_{\max}))$ ($g = g_{\min}, \dots, g_{\max} - 1$), are almost constant when a reaction occurs, where g_{\min} is the minimum value of the GOD (= 0).
 - ◆ Termination state (Stationary state)
 - The state that $p(g_{\max})$ is 1. This is the limit state when $t \rightarrow \infty$.
- **The above states can be modeled by a Markov chain.**

Effect of catalysts on GOD*

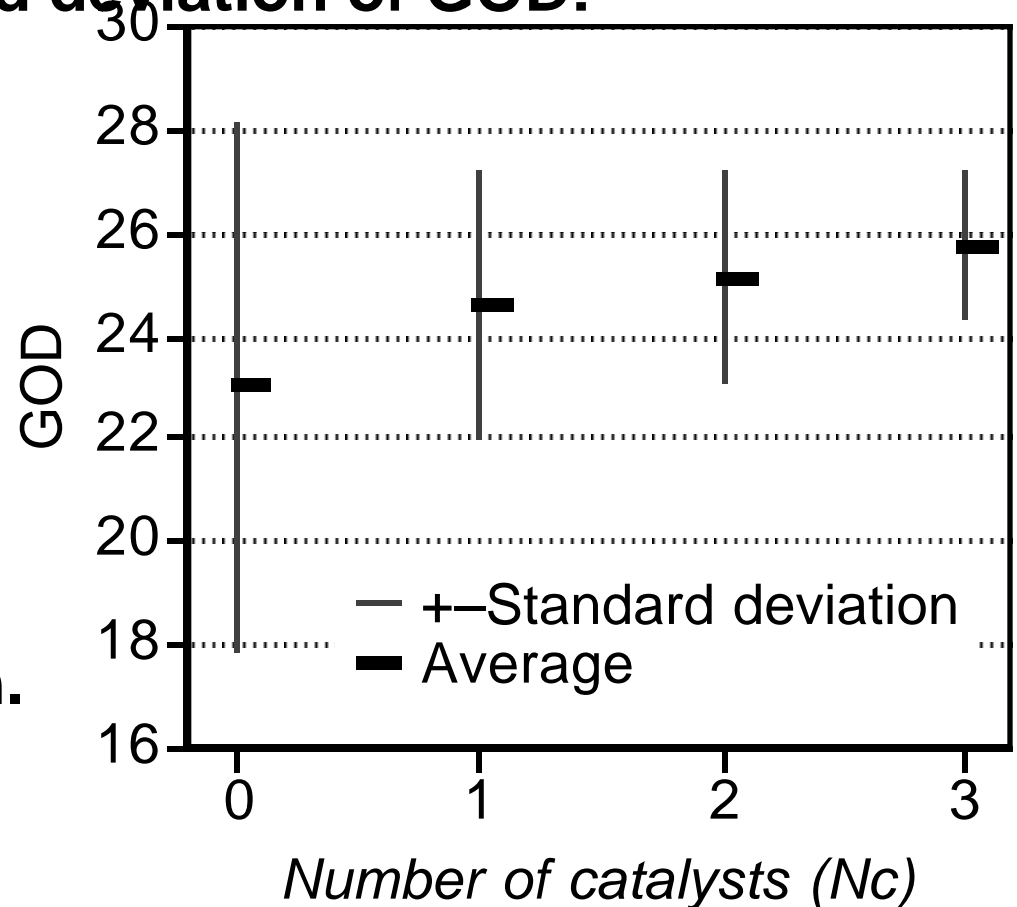
■ The average and standard deviation of GOD:

■ When N_c increases,

- ◆ The average becomes higher.
- ◆ The standard deviation becomes lower.

■ Catalysts bias the search.

- ◆ A rule with more catalysts searches among the states where the GOD is higher.
- ◆ So the number of reactions is smaller.



Conflict and Cooperation in CCM*

Categories of CCM-based systems

■ Cooperative systems

- ◆ No reaction will decrease the GOD in cooperative systems.
- ◆ Cooperative systems are called such because reactions cooperate toward the local or global maximum of the GOD.
- ◆ Examples: TSP system, the 0–1 Knapsack system and the sorting systems.

■ Conflicting systems

- ◆ A reaction may decrease the GOD in conflicting systems.
- ◆ Conflicting systems are called such because reactions does not cooperate toward that.
- ◆ Some systems have little conflict while others have considerably more.
- ◆ Examples: the N queens system and the graph coloring system.